

## Problem 9.33

A billiard ball of mass “m” hits a stationary billiard ball a glancing blow in an assumed “elastic collision.” As a consequence, its velocity magnitude becomes  $\vec{v}_r = (4.33 \text{ m/s}) \angle 30^\circ$ . Determine the blue ball’s final velocity.

This is another classic *conservation of momentum* problem. Using that, we can write:

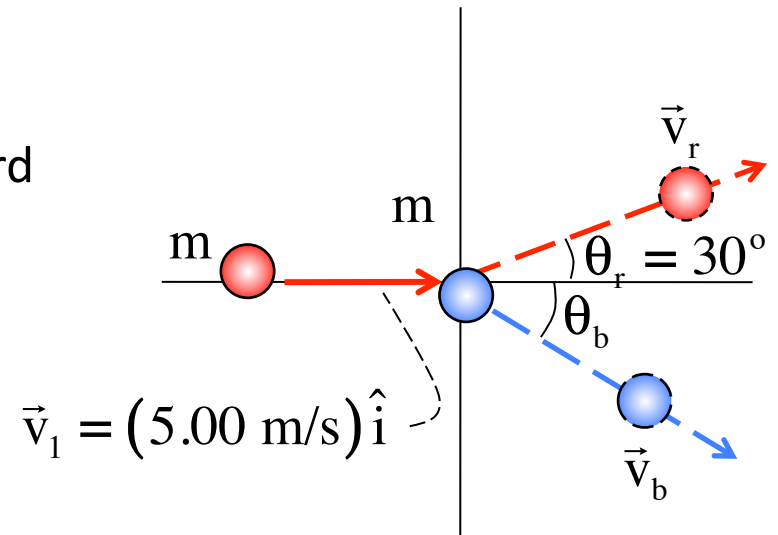
$$\sum p_{1,x} + \sum F_{\text{external},x} \Delta t_{\text{throughCollision}}^0 = \sum p_{2,x}$$

$$\Rightarrow m_r v_1 = m_r v_r \cos \theta_r + m_b v_b \cos \theta_b$$

$$\Rightarrow m(5.00 \text{ m/s}) = m(4.33 \text{ m/s}) \cos 30^\circ + m v_b \cos \theta_b$$

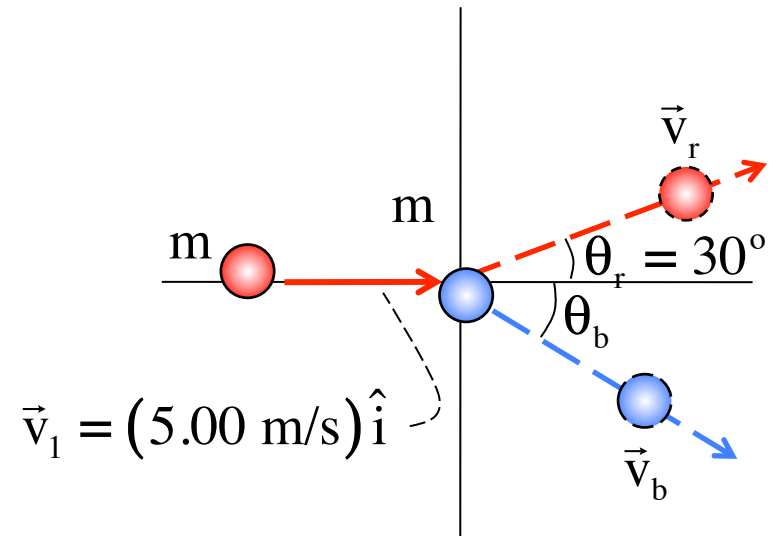
$$\Rightarrow v_b \cos \theta_b = (5.00 \text{ m/s}) - (4.33 \text{ m/s}) \cos 30^\circ$$

$$\Rightarrow v_b \cos \theta_b = 1.25 \text{ m/s}$$



With velocity signs unembedded to make the “v” terms magnitudes in the y-part of the *conservation of momentum*, we can write:

$$\begin{aligned}
\cancel{\sum p_{1,y}} + \cancel{\sum F_{\text{external},x} \Delta t_{\text{throughCollision}}} &= \sum p_{2,y} \\
\Rightarrow 0 &= m_r v_r \sin \theta_r - m_b v_b \sin \theta_b \\
\Rightarrow \cancel{m} v_b \sin \theta_b &= \cancel{m} (4.33 \text{ m/s}) \sin 30^\circ \\
\Rightarrow v_b \sin \theta_b &= (4.33 \text{ m/s}) \sin 30^\circ \\
\Rightarrow v_b \sin \theta_b &= 2.17 \text{ m/s}
\end{aligned}$$



Using the “dividing the two expressions” trick, we get:

$$\begin{aligned}
\frac{v_b \sin \theta_b}{v_b \cos \theta_b} &= \frac{(2.17 \text{ m/s})}{(1.25 \text{ m/s})} \\
\Rightarrow \tan \theta_b &= 1.74 \\
\Rightarrow \theta_b &= 60^\circ
\end{aligned}$$

This gives us a velocity magnitude of:

$$\begin{aligned}
v_b \sin 60^\circ &= 2.17 \text{ m/s} \\
\Rightarrow v_b &= 2.50 \text{ m/s}
\end{aligned}$$

Putting this information into a unit vector notation, we get:

$$\begin{aligned}\vec{v}_b &= (2.50 \text{ m/s}) \angle -60^\circ \\ &= [(2.50 \text{ m/s}) \cos 60^\circ] \hat{i} - [(2.50 \text{ m/s}) \sin 60^\circ] \hat{j} \\ &= (1.25 \text{ m/s}) \hat{i} - (2.17 \text{ m/s}) \hat{j}\end{aligned}$$

